



**What you already know**

- Relative atomic mass
- Relative molecular mass
- Dalton's atomic theory
- Law of conservation of mass
- Law of definite proportions
- Law of multiple proportions



**What you will learn**

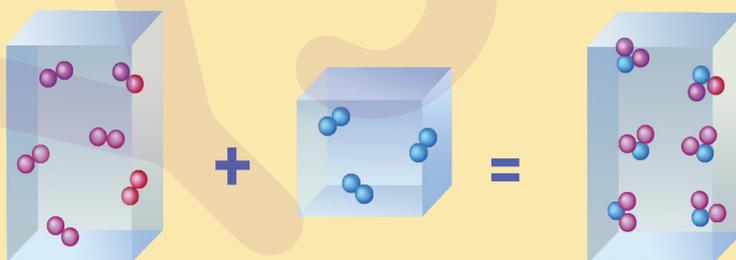
- Gay-Lussac's law
- Avogadro's law
- Relative density, Specific gravity and Vapour density
- Molar volumes at STP (NTP)



**Gay-Lussac's Law**

**Statement**

When **gases are combined or produced** in a chemical reaction, they do so in a **simple ratio by volume**, provided all gases are at the **same temperature and pressure**.



**Two volumes** of hydrogen combine with **one volume** of oxygen to give **two volumes** of water under the same **temperature and pressure**.

We already know, the mole ratio of the reactants and the products in a chemical reaction is in the whole number ratio.

According to **Gay-Lussac's law**, the volume ratio of the reactants and the products is also in the whole number ratio.



Here, **three volumes of hydrogen** combine with one volume of nitrogen to give two volumes of ammonia under the same temperature and pressure.



### To calculate the volume of gases using Gay-Lussac's law

What will be the respective **volumes of hydrogen** and **oxygen** consumed (in litres), if **20 litres** of  $\text{H}_2\text{O}(\text{g})$  is produced in the following reaction? (All gases are at the **same temperature and pressure**)



a) 10, 20

b) 20, 10

c) 40, 20

d) 20, 40

#### Solution

Given, Volume of  $\text{H}_2\text{O} = 20 \text{ L}$

Reaction conditions  $\rightarrow$  Same temperature and pressure

According to Gay-Lussac's law, at same temperature and pressure, the volume ratio of the reactants and the products is in the whole number ratio.

From the reaction,  $2\text{H}_2(\text{g}) + \text{O}_2(\text{g}) \rightarrow 2\text{H}_2\text{O}(\text{g})$ ,

Two volumes of hydrogen combine with one volume of oxygen to give two volumes of water.

For the production of 20 L of  $\text{H}_2\text{O}$ , 20 L of  $\text{H}_2$  combines with 10 L of  $\text{O}_2$ .

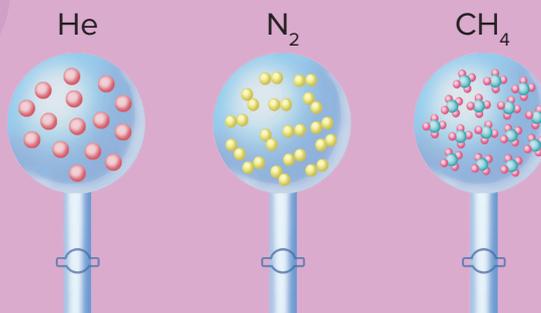
The correct option is **b**.



### Avogadro's Law

#### Statement

**Equal volumes** of gases at the **same temperature and pressure** should contain **equal** numbers of **molecules/particles**.



The **number of particles** in all the bulbs is **15** and the **volumes are identical**. This can also be stated as the **volume of gas is directly proportional to the number of particles at the same temperature and pressure**.

$$V \propto \text{Number of particles} \quad \frac{V_1}{n_1} = \frac{V_2}{n_2}$$

#### Relative Density (R.D.)

It is the density of a substance **relative** to the density of another substance at the **same T and P**. It is a dimensionless quantity.

$$\text{R.D.} = \frac{\rho_{\text{substance}}}{\rho_{\text{reference}}}$$

**R.D. is relative density** and  $\rho$  is **density**.

BOARDS

MAIN

ADVANCED

## Specific Gravity (S.G.)

Specific gravity for **liquids** is measured with respect to **water** at  $4^{\circ}\text{C}$ .

$$\text{S.G. (For liquids)} = \frac{\rho_{\text{substance}}}{\rho_{\text{water } 4^{\circ}\text{C}}}$$

**S.G.** is **specific gravity** and  $\rho$  is **density**.

For **gases**, it is measured with respect to **air** at **STP**.

$$\text{S.G. (For Gas)} = \frac{\rho_{\text{gas at STP}}}{\rho_{\text{air at STP}}}$$

It is a **dimensionless** quantity.

## Vapour Density (V.D.)

Density of the gas with respect to **hydrogen** gas at the **same temperature and pressure**. It indicates **how heavy a gas** is with respect to the **lightest gas**. It is also a **dimensionless** quantity.

$$\text{V.D.} = \frac{\text{Density of gas A at a given Temperature and Pressure}}{\text{Density of H}_2 \text{ gas at the same Temperature and Pressure}} \quad (\text{V.D. is vapour density})$$

$$\text{V.D.} = \frac{\text{Molar mass}}{2}$$

BOARDS

MAIN

## Molar Volume at STP

It is the volume occupied by **1 mole** of a gas.

**Molar volume at STP (Standard Temperature and Pressure)**

At STP condition: Temperature =  $0^{\circ}\text{C}$  or  $273\text{ K}$ ; Pressure =  $1\text{ bar}$ ; Molar volume at STP =  $22.7\text{ L}$   
 $1\text{ atm} = 1.01325\text{ bar}$

**Calculation of molar volume at STP**

$$\rho(\text{H}_2 \text{ at STP}) = 0.089\text{ g/L}$$

$$\text{Also, density} = \frac{M}{V_m}$$

$$0.089\text{ g/L} = \frac{2}{V_m}\text{ g/mol}$$

$$\text{Hence, molar volume, } V_m \text{ (in L/mol)} = \frac{2}{0.089}$$

$V_m = 22.7\text{ L}$  at **STP**; Temperature =  $0^{\circ}\text{C}$  or  $273\text{ K}$ ; Pressure =  $1\text{ bar}$  according to the new standard.

$V_m = 22.4\text{ L}$  at **STP**; Temperature =  $0^{\circ}\text{C}$  or  $273\text{ K}$ ; Pressure =  $1\text{ atm}$  according to the old standard.

**Molar volume at NTP (Normal Temperature and Pressure)**

At NTP condition: Temperature =  $20^{\circ}\text{C}$  or  $293\text{ K}$ ; Pressure =  $1\text{ atm}$ ; Molar volume at NTP =  $24\text{ L}$



## Finding the vapour density of a gas

Calculate the **vapour density of 20 g of methane gas**.

**Solution**

$$\text{Vapour density} = \frac{\text{Molar mass}}{2}$$

Molar mass of methane ( $\text{CH}_4$ ) =  $12 + (1 \times 4) = 16 \text{ g}$

Hence, vapour density of methane =  $\frac{16}{2} = 8$



Vapour density **does not depend** upon the **mass of a gas**.

**Finding the vapour density of a gas**

The **relative density** of **gas A** with respect to another **gas B** is **2**. If the **vapour density** of **gas B** is **20**, find the **vapour density of gas A**.

**Solution****Step 1:****Finding the molar mass of gas B ( $M_B$ )**

Given,

Vapour density of gas B = 20

$$\text{V.D.} = \frac{M_B}{2} = 20$$

$$M_B = 40 \text{ g}$$

**Step 3:****Finding the vapour density of gas A**

$$\text{Vapour density} = \frac{\text{Molar mass}}{2}$$

$$\therefore \text{Vapour density of gas A} = \frac{80}{2} = 40$$

**Step 2:****Finding the molar mass of gas A ( $M_A$ )**

Relative density of gas A =

$$\frac{\text{Density of gas A at a T and P}}{\text{Density of gas B at the same T and P}}$$

$$\frac{\text{Mass of 1 mole of gas A at a T and P}}{\text{Mass of 1 mole of gas B at the same T and P}}$$

$$\Rightarrow 2 = \frac{\text{Molar mass of A}}{\text{Molar mass of B}} = \frac{M_A}{M_B} = \frac{M_A}{40}$$

$$M_A = 80 \text{ g}$$

**Finding the vapour density of a gaseous mixture**

Calculate the **vapour density** of a mixture containing **44 g of  $\text{CO}_2$**  and **30 g of ethane**.

**Solution****Step 1:****Finding the moles of the components**

Given,

Mass of  $\text{CO}_2$  = 44 g

Mass of ethane = 30 g

Molar mass of ethane ( $\text{C}_2\text{H}_6$ ) = 30 g

$$\begin{aligned} \text{Moles of } \text{CO}_2 &= \frac{\text{Given mass}}{\text{Molar mass}} \\ &= \frac{44 \text{ g}}{44 \text{ g}} = 1 \text{ mol} \end{aligned}$$

$$\begin{aligned} \text{Moles of } \text{C}_2\text{H}_6 &= \frac{\text{Given mass}}{\text{Molar mass}} \\ &= \frac{30 \text{ g}}{30 \text{ g}} = 1 \text{ mol} \end{aligned}$$

**Step 2:****Finding the average molar mass**

$$\text{Total mass} = (44 + 30) \text{ g} = 74 \text{ g}$$

$$\text{Total moles} = n_{\text{CO}_2} + n_{\text{C}_2\text{H}_6} = 1 + 1 = 2$$

Average Molar mass

$$= \frac{\text{Total mass}}{\text{Total moles}} = \frac{74 \text{ g}}{2} = 37 \text{ g}$$

**Step 3:****Finding vapour density**

∴ Vapour density of mixture

$$\frac{\text{Molar mass}}{2} = \frac{37}{2} = 18.5$$

**Finding the ratio of molar mass from the ratio of vapour density**

**Vapour density** of two gases is in the ratio of **1 : 3**. What will be the **ratio of their molar masses**?

**Solution**

Let the two gases be A and B.

$$\frac{\text{Vapour density of gas A}}{\text{Vapour density of gas B}} = \frac{1}{3}$$

$$\text{Vapour density} = \frac{\text{Molar mass}}{2}$$

$$\frac{(\text{Molar mass of gas A})/2}{(\text{Molar mass of gas B})/2} = \frac{1}{3}$$

$$\frac{\text{Molar mass of gas A}}{\text{Molar mass of gas B}} = \frac{1}{3}$$

Hence, the ratio of the molar masses of gas A and gas B respectively is 1 : 3.

**Finding the number of molecules from the number of moles**

Gas A has a vapour density of 8.55. Find the **number of molecules** in **0.5 mol** of the gas.

**Solution**

Given: Number of moles of gas A = 0.5 mol

$$\text{No. of moles} = \frac{\text{Number of Particles (given)}}{N_A}$$

$$0.5 = \frac{\text{Number of molecules}}{N_A}$$

$$\text{Hence, number of molecules} = 0.5 N_A$$

**Finding the vapour density from mass**

A gas cylinder holds **85 g of gas X**. The **same** cylinder, when filled with **hydrogen**, holds **8.5 g** of **H<sub>2</sub>** at the same temperature. Find its **vapour density**.

**Solution**

Let the volume of the cylinder be 'V' mL.

Given,

Mass of gas X in 'V' mL = 85 g

Mass of gas H<sub>2</sub> in 'V' mL = 8.5 g (at the same temperature)

$$\text{Vapour density} = \frac{\text{Mass of gas X / V mL at some T and P}}{\text{Mass of H}_2 \text{ gas / V mL at some T and P}} = \frac{85}{8.5} = 10$$

(Volume **V mL** is the same for both the gases as they are present in the same cylinder.)



### Finding the vapour density of a mixture

A gaseous mixture of H<sub>2</sub> and CO<sub>2</sub> gas contains **66% by mass of CO<sub>2</sub>**. What is the **vapour density** of the mixture?

#### Solution

##### Step 1:

##### Finding the moles of all components

Let the mass of the mixture = 100 g

Given,

Mass of CO<sub>2</sub> in the mixture = 66% of 100 g  
= 66 g

Mass of H<sub>2</sub> = (100 - 66) g = 34 g

$$\text{Moles of CO}_2 = \frac{\text{Given mass}}{\text{Molar mass}}$$

$$= \frac{66 \text{ g}}{44 \text{ g}} = 1.5 \text{ mol}$$

$$\text{Moles of H}_2 = \frac{\text{Given mass}}{\text{Molar mass}}$$

$$= \frac{34 \text{ g}}{2 \text{ g}} = 17 \text{ mol}$$

##### Step 2:

##### Finding the average molar mass

Total mass = 100 g

Total moles = 1.5 + 17 = 18.5 mol

Average Molar mass

$$= \frac{\text{Total mass}}{\text{Total moles}} = \frac{100}{18.5} = 5.41 \text{ g}$$

##### Step 3:

##### Finding the vapour density

$$\text{Vapour density} = \frac{\text{Molar mass}}{2}$$

$$= \frac{5.41}{2} = 2.7$$



### Vapour density calculation

**0.24 g of a volatile liquid** on vaporisation gives **45 mL of vapours at STP**. What will be the **vapour density** of the substance? (Density of H<sub>2</sub> = 0.089 g L<sup>-1</sup>)

a) 95.39

b) 39.95

c) 99.53

d) 59.73

#### Solution

$$\text{V.D.} = \frac{\text{Density of substance at a given temperature \& pressure}}{\text{Density of H}_2 \text{ gas at the same temperature \& pressure}}$$

Given,

Density of hydrogen = 0.089 g L<sup>-1</sup>

$$\text{Density of volatile liquid} = \frac{\text{Mass in g}}{\text{Volume in L}} = \frac{0.24 \text{ g}}{45 \times 10^{-3} \text{ L}}$$

$$\text{V.D.} = \frac{0.24 \text{ g} / 45 \times 10^{-3} \text{ L}}{0.089 \text{ g L}^{-1}} = 59.73$$

Option d is correct.



### Calculating the molar composition from vapour density

A gaseous mixture of  $\text{D}_2$  and  $\text{CO}_2$  gas has a vapour density of 12. Calculate the molar composition of the mixture.

#### Solution

##### Step 1:

##### Finding the average molar mass

Given,

$$\text{V.D.} = 12$$

$$\text{We know V.D.} = \frac{\text{Molar mass}}{2}$$

$$\text{So, } M_{\text{avg}} = 24 \text{ g}$$

where **V.D.** is vapour density and **M<sub>avg</sub>** is average molar mass.

##### Step 2:

##### Finding the molar composition of mixture

Let us consider 1 mol mixture of  $\text{D}_2$  and  $\text{CO}_2$ ,  $x$  moles of  $\text{D}_2$  and  $(1 - x)$  moles of  $\text{CO}_2$ .

$$m(\text{D}_2) + m(\text{CO}_2) = 24 \text{ g}$$

$$\text{Molar mass of } \text{D}_2 \times x + \text{Molar mass of } \text{CO}_2 \times (1 - x) = 24$$

$$4x + 44 \times (1 - x) = 24$$

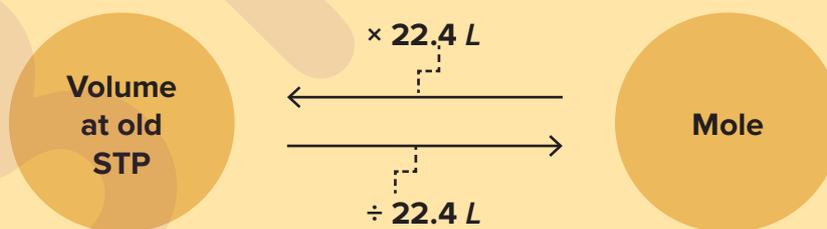
$$x = 0.5$$

$$\text{Number of moles of } \text{D}_2 = x \text{ mol} = 0.5 \text{ mol}$$

$$\text{Number of moles of } \text{CO}_2 = (1 - x) \text{ mol} = 0.5 \text{ mol}$$



### Interconversion of Mole-Volume



- **22.4 L** of any gas at **STP (1 atm, 0°C)** is the molar volume (**V<sub>m</sub>**, volume of one mole of gas).
- **11.2 L** of a gas at STP has 0.5 moles.
- **2 moles** of a gas at STP contains **44.8 L** volume.

$$\text{Number of moles} = \frac{\text{Volume of gas (L, STP)}}{\text{Molar volume (22.4 L)}} = \frac{\text{Volume of gas (mL, STP)}}{22400 \text{ mL}}$$



### Mole-Volume interconversion

What **volume** would **0.735 moles of O<sub>2</sub>** gas occupy at **1 atm and 0°C**?

**Solution**

In the question STP condition is given.

So, **using the interconversion of mole-volume relationship**, we have,  $V \text{ (STP)} = n \times 22.4 \text{ L}$

So,  $V = 22.4 \times 0.735 = 16.46 \text{ L}$

**Mole-Volume interconversion**

How many moles are there in **11.2 L of CO<sub>2</sub>** gas at STP?

a) **0.5 mol of C atoms**

b) **1 mol of O atoms**

c) **0.5 mol of CO<sub>2</sub> molecules**

d) **4 mol of total atoms**

**Solution**

Using the interconversion of mole-volume relationship,

The number of moles,  $n = \frac{\text{Volume gas (at STP)}}{22.4 \text{ L}}$

$$n = \frac{11.2}{22.4} = 0.5 \text{ mol}$$

a) 1 mole of CO<sub>2</sub> contains 1 mole of carbon atoms. So, 0.5 moles of CO<sub>2</sub> contain 0.5 moles of carbon atoms.

b) 1 mole of CO<sub>2</sub> contains 2 moles of oxygen atoms. So, 0.5 moles of CO<sub>2</sub> contain 1 mole of oxygen atoms.

c) Number of moles of CO<sub>2</sub> molecules = 0.5 mol

d) Total number of atoms in a CO<sub>2</sub> molecule is 3. So, 0.5 moles of CO<sub>2</sub> molecules contain 1.5 mol of total atoms.

Options **a, b, and c** are correct.

**Mole-Volume interconversion**

How many moles are there in **29.4 L of liquid ethanol** at STP?

a) **1.31 mol**

b) **1.6 mol**

c) **1.1 mol**

d) **Cannot be determined**

**Solution**

Volume of gas occupied at STP = 22.4 L

Using the **interconversion of mole-volume relationship**,

In the formula of mole-volume interconversion, we deal the volume of the gas.

The number of moles,  $n = \frac{\text{Volume of the gas}}{22.4 \text{ L}}$

However, in the given question, since the volume of liquid is given, the number of moles cannot be determined.

Correct option is d.



### Interconversion of Mole-Volume



- If the mass of a gas is given,

$$\text{Moles} = \frac{\text{Given Mass}}{\text{Molar Mass}}$$

$$\begin{aligned} \text{Volume of gas (L)} &= \text{Moles} \times \text{Molar volume} \\ &= \text{Moles} \times 22.4 \end{aligned}$$

- If the volume of gas is given,

$$\text{Moles} = \frac{\text{Volume of gas (L)}}{22.4 \text{ L}}$$

$$\text{Mass} = \text{Moles} \times \text{Molar mass}$$



#### Mass-Volume interconversion

What **volume (in L)** is occupied by **60 g of ethane at STP**?

##### Solution

##### Step 1:

Finding the number of moles of ethane using the formula,

$$n = \frac{\text{Given mass}}{\text{Molar Mass}} = 60/30 = 2 \text{ mol}$$

##### Step 2:

Using the interconversion of mole-volume relationship,

$$V \text{ (STP, L)} = n \times 22.4$$

$$V = 22.4 \text{ L} \times 2 = 44.8 \text{ L}$$



#### Mass-Mole-Volume interconversion and molecular formula determination

**16 g** of an ideal gas **SO<sub>x</sub>** occupies **5.6 L at STP**. Find the value of **x**.

##### Solution

##### Step 1:

Finding the number of moles of **SO<sub>x</sub>** gas

Using the interconversion of mole-volume relationship,

We have, the number of moles,

$$n = \frac{\text{Volume gas (at STP)}}{22.4 \text{ L}}$$

$$n = \frac{5.6}{22.4} = 0.25 \text{ mol}$$

##### Step 2:

Finding the value of **x**

0.25 mol of gas contains 16 g of an ideal gas, **SO<sub>x</sub>**.

Then, 1 mol of gas will contain 64 g of **SO<sub>x</sub>**.

Thus, 64 g is the molar mass of **SO<sub>x</sub>**.

$$32 + 16x = 64$$

$$x = 2$$

BOARDS

MAIN

## Interconversion of Mole-Volume



If the number of particles of a gas are given,

$$\text{Moles} = \frac{\text{Number of particles}}{N_A}$$

$$\text{Number of particles} = \text{Moles} \times N_A$$

If volume of gas is given,

$$\text{Moles} = \frac{\text{Volume of gas (L)}}{22.4 \text{ L}}$$

$$\text{Volume of gas (L)} = \text{Moles} \times 22.4 \text{ L}$$



## Finding the volume from the number of atoms

Calculate the **volume** occupied by **Cl<sub>2</sub> gas** at **STP** (atm) if the number of **Cl atoms** is the **same** as the number of **O atoms** present in **4.8 g ozone**.

## Solution

## Step 1:

## Finding the number of oxygen atoms in ozone

$$\text{Number of moles (n)} = \frac{\text{Given mass (m)}}{\text{Molar Mass (M)}}$$

Given mass of ozone = 4.8 g

Molar mass of ozone =  $3 \times 16 = 48 \text{ g/mol}$

$$n = \frac{4.8}{48} = 0.1 \text{ mol of ozone molecules}$$

1 mol of ozone molecule contains 3 atoms of oxygen.

So, by unitary method, 0.1 mol of ozone

molecules will contain  $0.1 \times \frac{3}{1}$ , i.e., 0.3 moles of oxygen atoms.

## Step 2:

Finding the number of molecules of Cl<sub>2</sub> gas

Given that the number of Cl atoms is the same as the number of O atoms, i.e., 0.3 mol.

1 molecule of chlorine contains 2 atoms.

So, by unitary method, the number of Cl<sub>2</sub> molecules present in 0.3 mol of Cl atoms is  $\frac{0.3}{2}$ , i.e., 0.15 mol

## Step 3:

Finding the volume occupied by Cl<sub>2</sub> gas

$$V (\text{STP, L}) = n \times 22.4$$

$$V = 22.4 \text{ L} \times 0.15 = 3.36 \text{ L}$$



## Particles-Volume interconversion

**4.4 g of CO<sub>2</sub>** and **2.24 L of H<sub>2</sub>** at **STP** are mixed in a container. Find the **total number of molecules** present in the container.

a)  $6.02 \times 10^{23}$

b)  $12.04 \times 10^{22}$

c) 2 moles

d)  $6.02 \times 10^{24}$

**Solution****Step 1:****Finding the number of moles of CO<sub>2</sub>**

Using the interconversion of mole-mass relationship,

We have, the number of moles,

$$n = \frac{\text{Given mass}}{\text{Molar mass}}$$

$$n = \frac{4.4}{44} = 0.1 \text{ mol}$$

**Step 2:****Finding the number of moles of H<sub>2</sub>**

Using the interconversion of mole-volume relationship,

We have, the number of moles,

$$n = \frac{\text{Volume of gas (at STP, L)}}{22.4 \text{ L}}$$

$$n = \frac{2.24}{22.4} = 0.1 \text{ mol}$$

**Step 3:****Total number of molecules**

Total number of moles carbon dioxide and hydrogen gas = 0.2 mol

The total number of atoms =  $0.2 \times N_A = 12.046 \times 10^{22}$

**Particles-Volume interconversion**

From **160 g of a SO<sub>2</sub>(g)** sample,  **$1.2046 \times 10^{24}$  molecules of SO<sub>2</sub>** are removed. Find the **volume** of the left over **SO<sub>2</sub>(g)** at STP.

**Solution****Step 1:****Finding the number of moles of SO<sub>2</sub>**

Using the interconversion of mole-mass relationship,

The number of moles

$$n = \frac{\text{Given mass}}{\text{Molar mass}}$$

$$n = \frac{160}{64} = 2.5 \text{ mol}$$

**Step 2:****Finding moles of SO<sub>2</sub> removed**

Now, the number of moles of SO<sub>2</sub> removed

$$= \frac{1.2046 \times 10^{24}}{N_A}$$

$$= \frac{1.2046 \times 10^{24}}{6.023 \times 10^{23}} = 2 \text{ mol}$$

**Step 3:****Number of moles remaining**

The number moles remaining  
=  $2.5 - 2 = 0.5$

**Step 4:****Volume of left over SO<sub>2</sub>**

Volume of left over SO<sub>2</sub> =  $n \times 22.4 \text{ L}$   
 $V = 0.5 \times 22.4 = 11.2 \text{ L}$

**Finding the volume from the number of electrons present in the sample**

A pure sample of CO<sub>2</sub> contains a total of  **$2.2 \times 10^{10}$  electrons**. Find the **volume occupied by CO<sub>2</sub> at STP (atm)**.

**Solution****Step 1:****Finding the number of molecules of CO<sub>2</sub>**

Number of electrons present in a CO<sub>2</sub> molecule =  $6 + (8 \times 2) = 22$  electrons

By unitary method,  $2.2 \times 10^{10}$  electrons will be present in  $2.2 \times 10^{10} \times \frac{1}{22}$ , i.e.,  $10^9$  molecules.

**Step 2:****Finding the moles of CO<sub>2</sub>**

$$\begin{aligned} \text{Number of moles (n)} &= \frac{\text{Number of molecules}}{N_A \text{ (Avogadro's number)}} \\ &= \frac{10^9}{6.023 \times 10^{23}} = 1.66 \times 10^{-15} \text{ mol} \end{aligned}$$

**Step 3:****Finding the volume occupied by CO<sub>2</sub>**

Volume of gas occupied at STP = 22.4 L

Volume of gas,  $V = \text{moles} \times 22.4 \text{ L}$

$V \text{ (STP, L)} = n \times 22.4$

$V = 22.4 \times 1.66 \times 10^{-15} = 3.71 \times 10^{-14} \text{ L}$



### Interconversion of Mole-Volume, Mass, and Number of Particles

